

# FAT-GPU: Formal Analysis Techniques for GPU kernels

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Supported by the FP7 project CARP: Correct and Efficient Accelerator Programming

# Aims of this tutorial

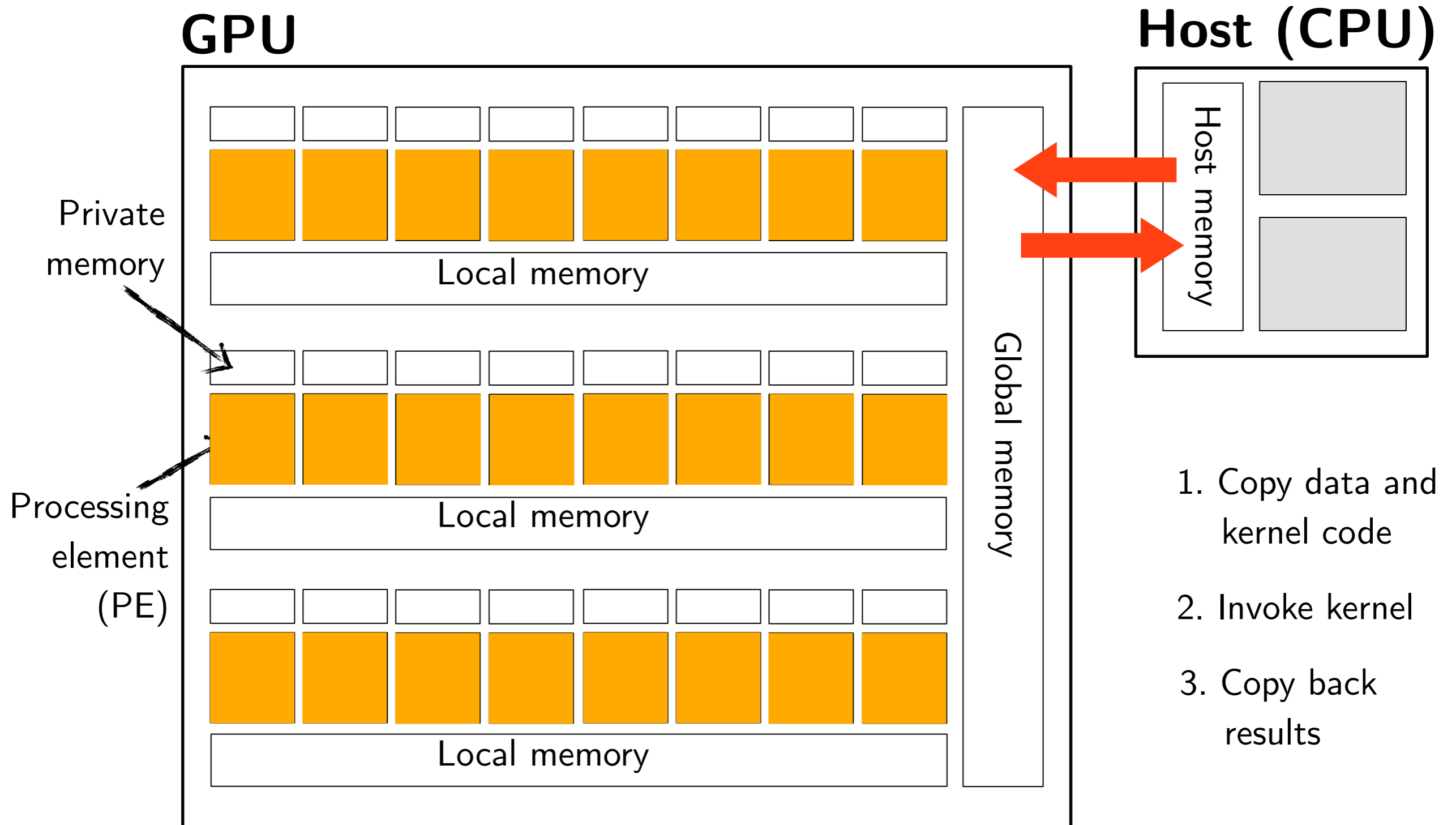
- ▶ Explain two pitfalls of GPU programming: **data races** and **barrier divergence**
- ▶ Demonstrate **GPUVerify**, a tool for statically analysing GPU kernels to check for these kinds of defects
- ▶ Introduce some of the verification techniques underlying GPUVerify
- ▶ (Compare with another GPU verification tool)

# GPUs and GPU programming

# GPUs

- ▶ Many parallel processing elements
- ▶ Originally designed to accelerate graphics processing, limited functionality, hard to program
- ▶ Recently, more general-purpose functionality. Accelerate such tasks as:
  - Medical imaging
  - Computational fluid dynamics
  - Financial simulation
  - DNA sequence alignment
  - Computer vision
  - ... and many more

# GPU Architecture

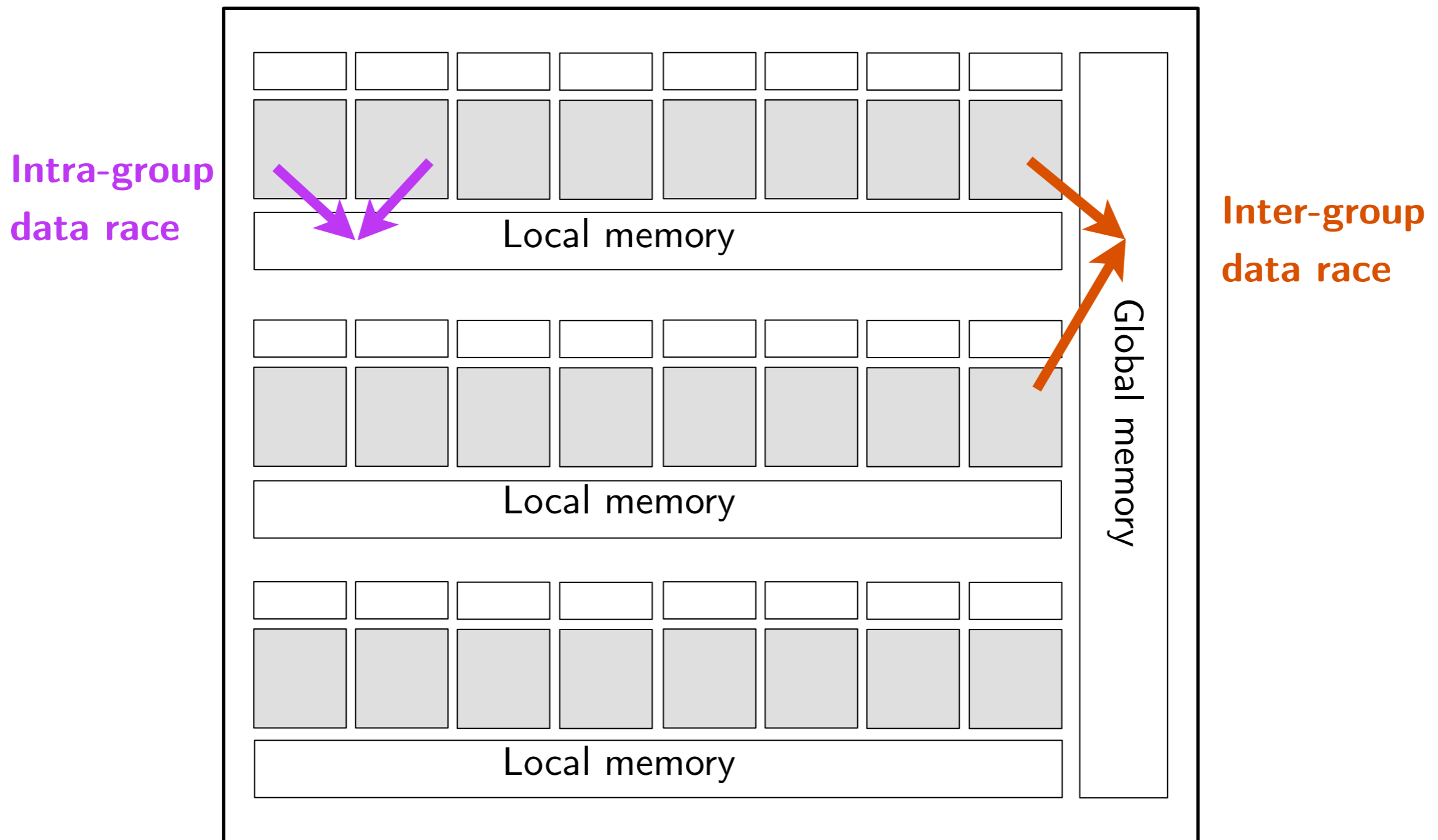


# Data races

- ▶ A **data race** occurs when:
  - two **different** threads access the **same** memory location
  - at least one of the accesses is a **write**
  - the accesses are **not** separated by a **barrier**

# Data races

## GPU



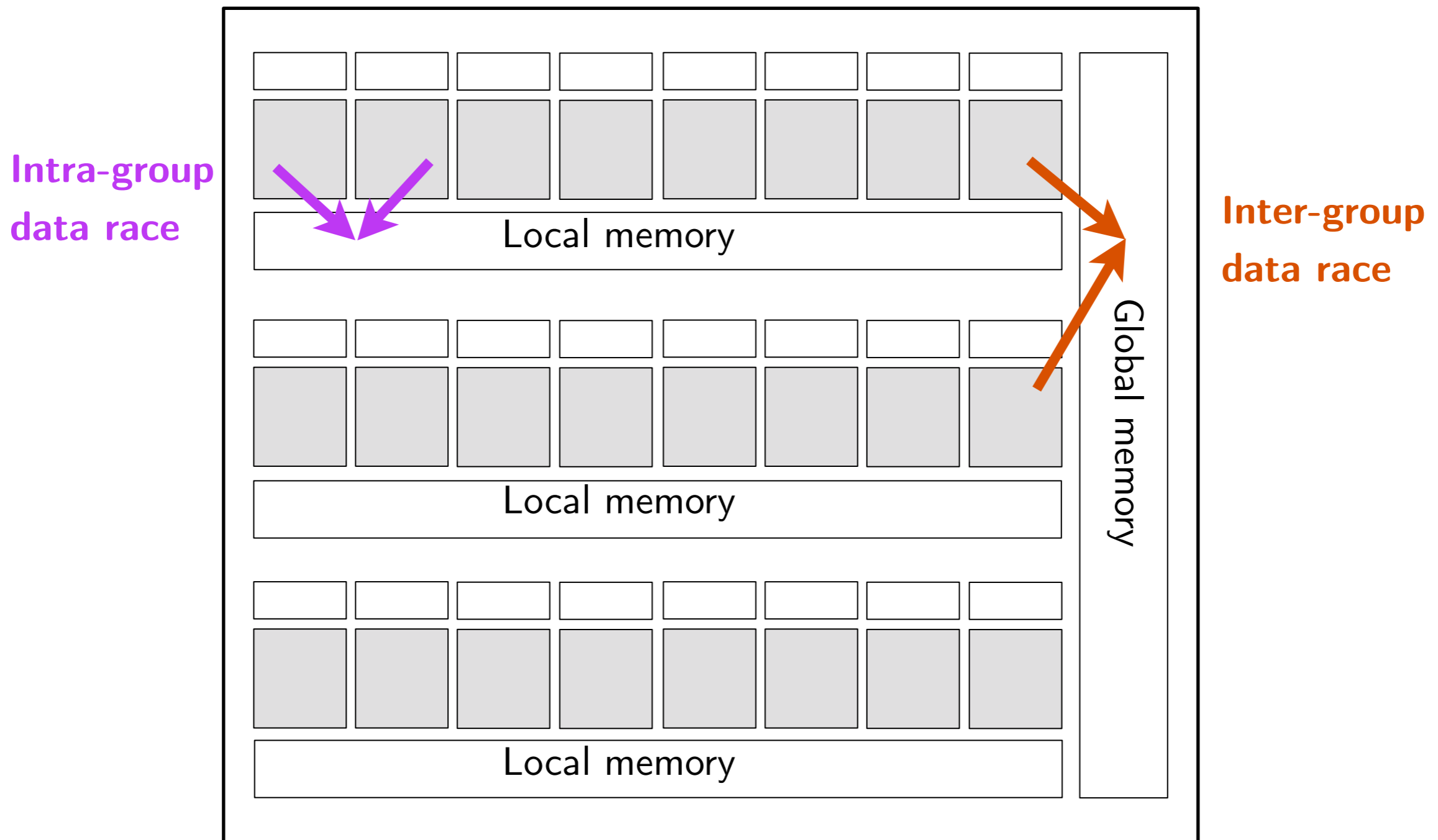
# Data races

- ▶ A **data race** occurs when:
  - two **different** threads access the **same** memory location
  - at least one of the accesses is a **write**
  - the accesses are **not** separated by a **barrier**
- ▶ Data races can cause **undefined behaviour**
- ▶ Almost always **accidental** and **unwanted**



# Data races

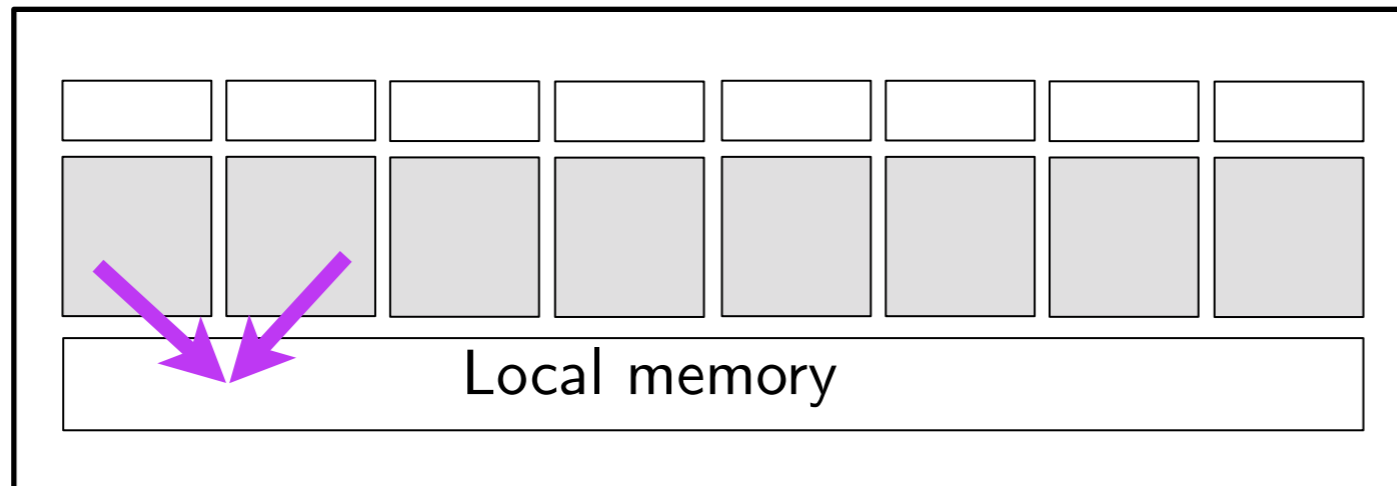
## GPU



# Data races

**GPU**

Intra-group  
data race



# A GPU kernel

This function is the kernel's entry point

The array A is stored in the group's local memory

```
#define tid (get_local_id(0))  
  
__kernel void  
add_neighbour(__local int* A, int offset) {  
    A[tid] = A[tid] + A[tid + offset];  
}
```

Identifies the current thread

# A GPU kernel

```
__kernel void  
add_neighbour(__local int* A, int offset) {  
    A[tid] = A[tid] + A[tid + offset];  
}
```

- ▶ Suppose `offset = 1`, and that there are four threads

Thread:	0	1	2	3
Reads:	A[0]	A[1]	A[2]	A[3]
	A[1]	A[2]	A[3]	A[4]
Writes:	A[0]	A[1]	A[2]	A[3]

data race

# Effects of a data race

- ▶ Suppose `offset = 1`, and that there are four threads

A[0]	A[1]	A[2]	A[3]	A[4]
1	1	1	1	1

Thread 0

2	1	1	1	1
---	---	---	---	---

Thread 1

2	2	1	1	1
---	---	---	---	---

Thread 2

2	2	2	1	1
---	---	---	---	---

Thread 3

2	2	2	2	1
---	---	---	---	---

A[0]	A[1]	A[2]	A[3]	A[4]
1	1	1	1	1

Thread 3

1	1	1	2	1
---	---	---	---	---

Thread 2

1	1	3	2	1
---	---	---	---	---

Thread 1

1	4	3	2	1
---	---	---	---	---

Thread 0

5	4	3	2	1
---	---	---	---	---

# Barrier synchronisation

- ▶ No thread can proceed beyond a `barrier()` until all threads have reached it
- ▶ Reads and writes from before the barrier are guaranteed to have completed after the barrier

```
__kernel void  
add_neighbour(__local int* A, int offset) {  
    int tmp = A[tid] + A[tid + offset];  
    barrier();  
    A[tid] = tmp;  
}
```

# Barrier divergence

- ▶ Threads must reach the same barrier

```
__kernel void foo() {  
    if (tid == 0)  
        barrier();  
    else  
        barrier();  
}
```

**NOT ALLOWED**

# Barrier divergence

- ▶ Threads must reach the same barrier
- ▶ If the barrier is in a loop, threads must have performed the same number of iterations upon reaching it

```
__kernel void foo() {  
    int i_max = (tid==0 ? 4 : 1);  
    int j_max = (tid==0 ? 1 : 4);  
    for (int i = 0; i < i_max; i++)  
        for (int j = 0; j < j_max; j++)  
            barrier();  
}
```

**NOT ALLOWED**

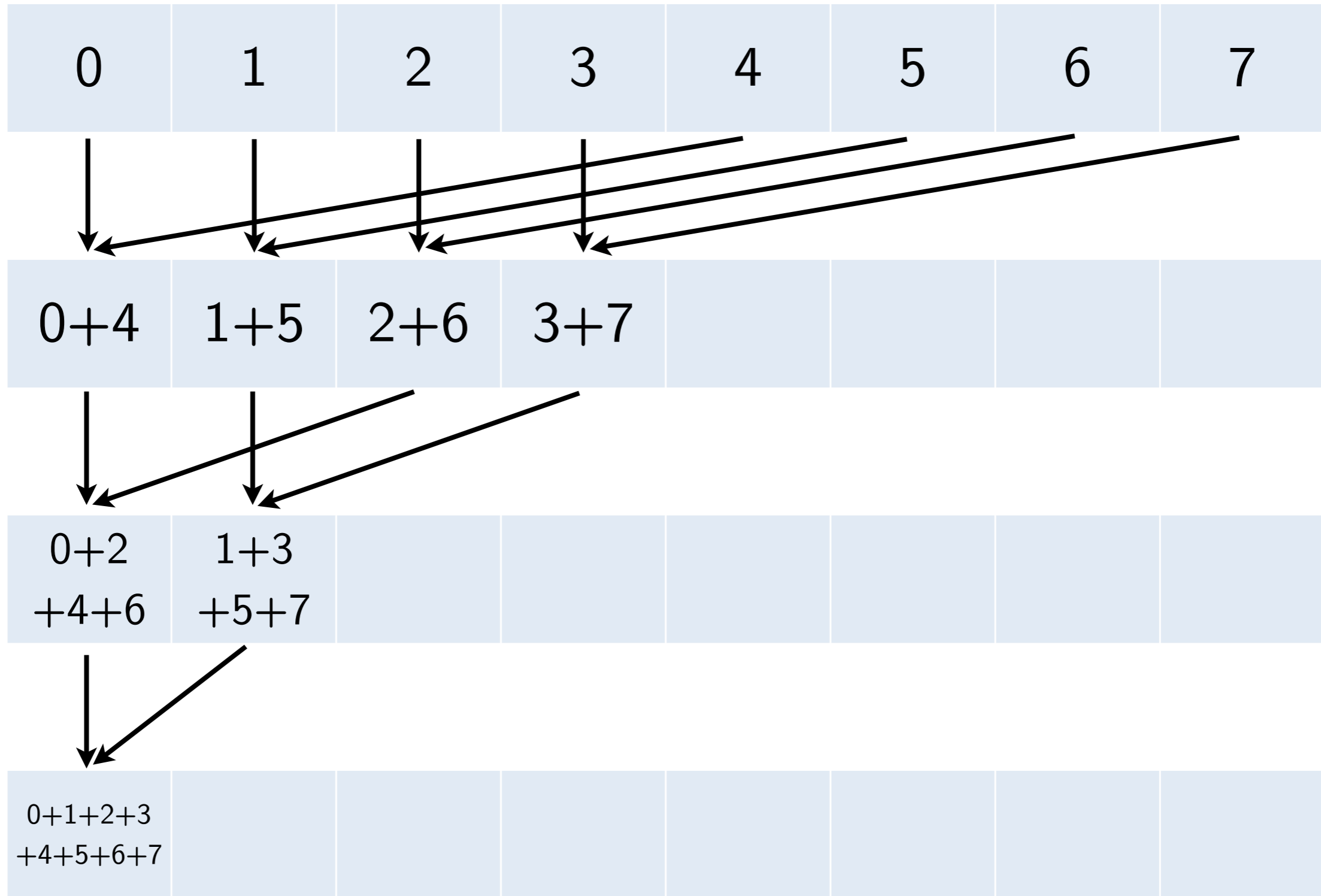


# The GPUVerify tool

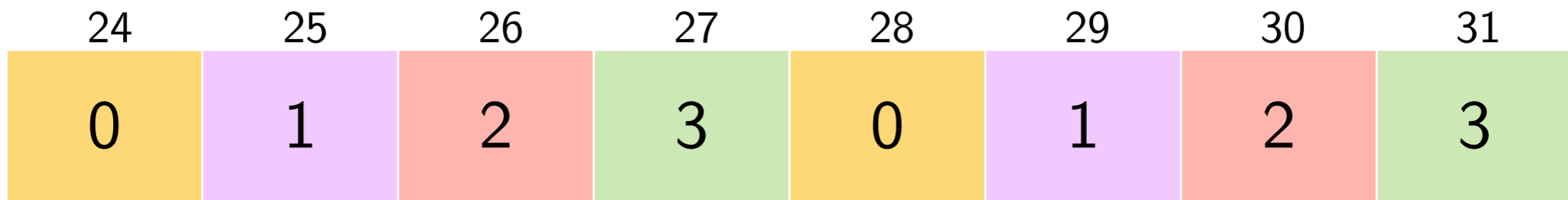
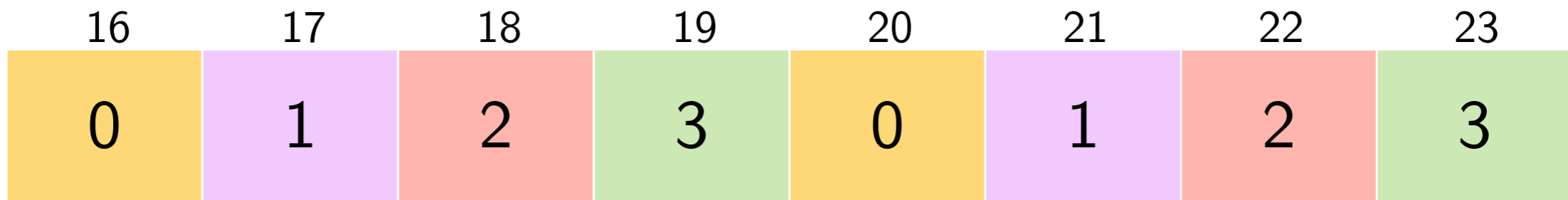
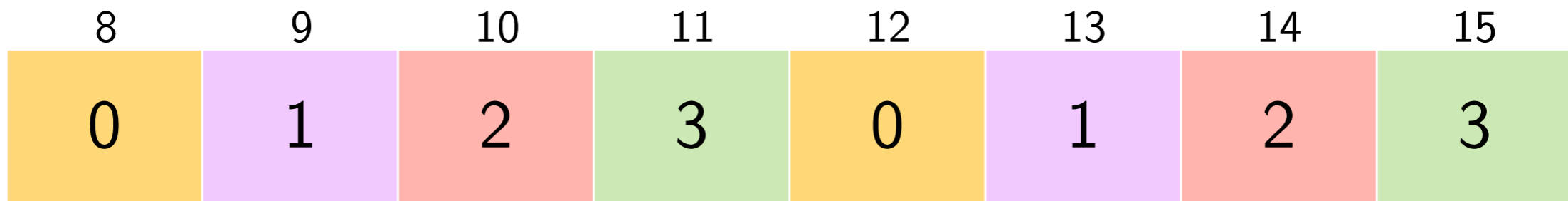
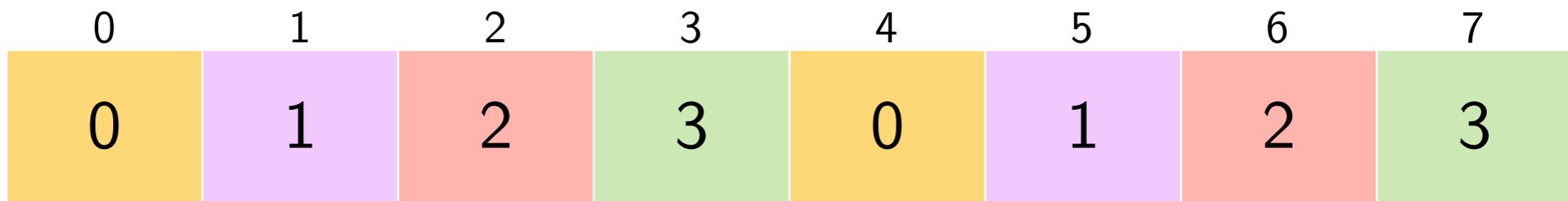
# The GPUVerify tool

- ▶ A verifier for GPU kernels
- ▶ Analyses the source code of OpenCL and CUDA kernels to check for:
  - Intra-group and inter-group data races
  - Barrier divergence
  - Violations of user-specified assertions
- ▶ Download from [multicore.doc.ic.ac.uk/tools/GPUVerify](http://multicore.doc.ic.ac.uk/tools/GPUVerify)
- ▶ Or try it online at [rise4fun.com/GPUVerify-OpenCL](http://rise4fun.com/GPUVerify-OpenCL)

# Parallel reduction

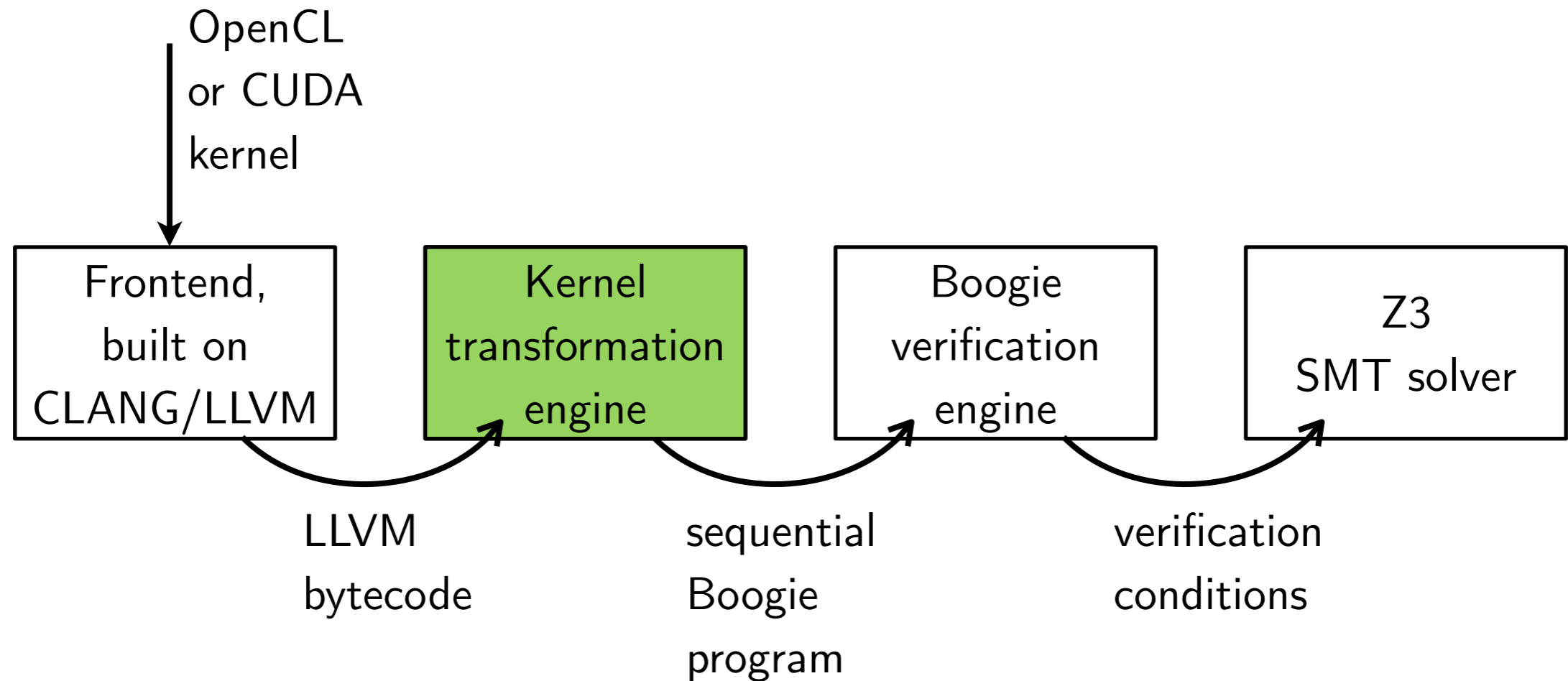


# Striding



# How the GPUVerify tool works

# Architecture of GPUVerify



# Verification technique

► Plan:

Transform massively-parallel kernel **K**  
into a sequential program **P**  
such that if **P** is correct  
then **K** has no data races  
and no barrier divergence.

# Making the problem tractable

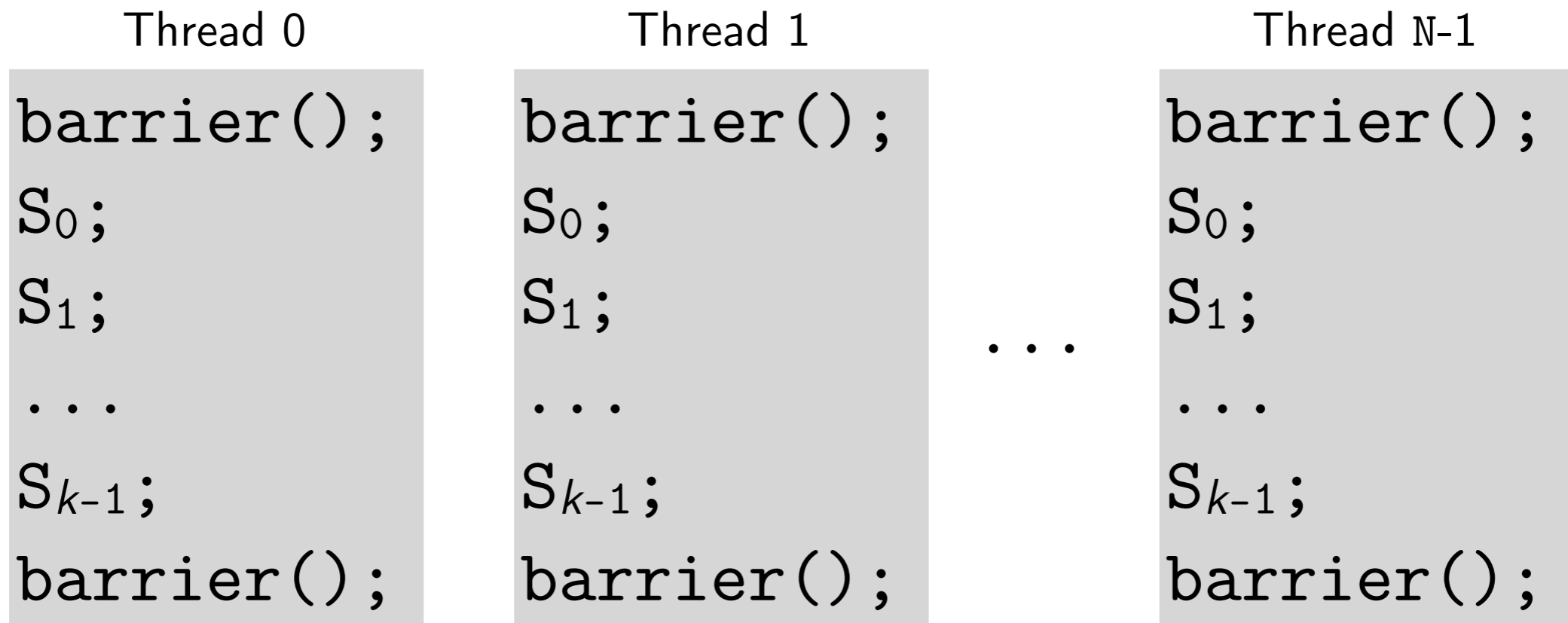
- ▶ Data race analysis focuses on each barrier-separated region separately

```
barrier();  
S0;  
S1;  
...  
Sk-1;  
barrier();
```



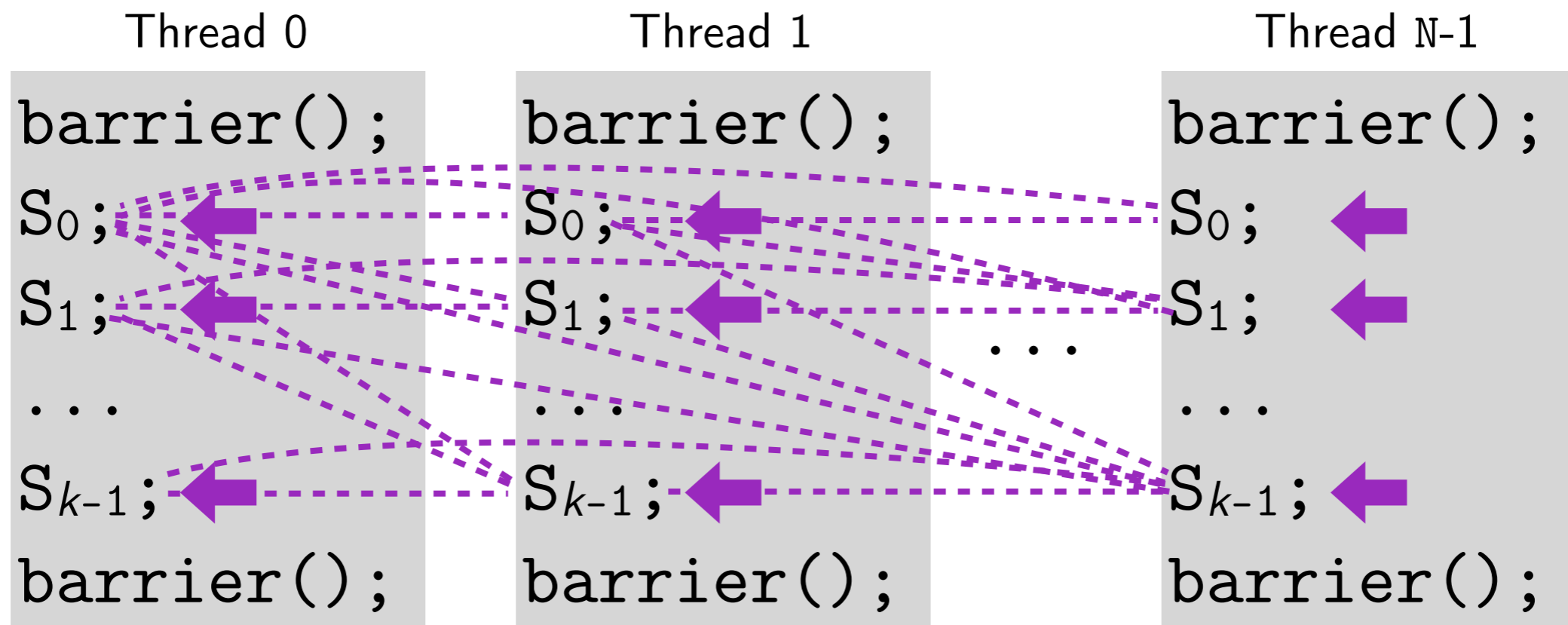
# Making the problem tractable

- ▶ There are about  $N^k$  possible interleavings ...  
but **any one of them** will do!



# Making the problem tractable

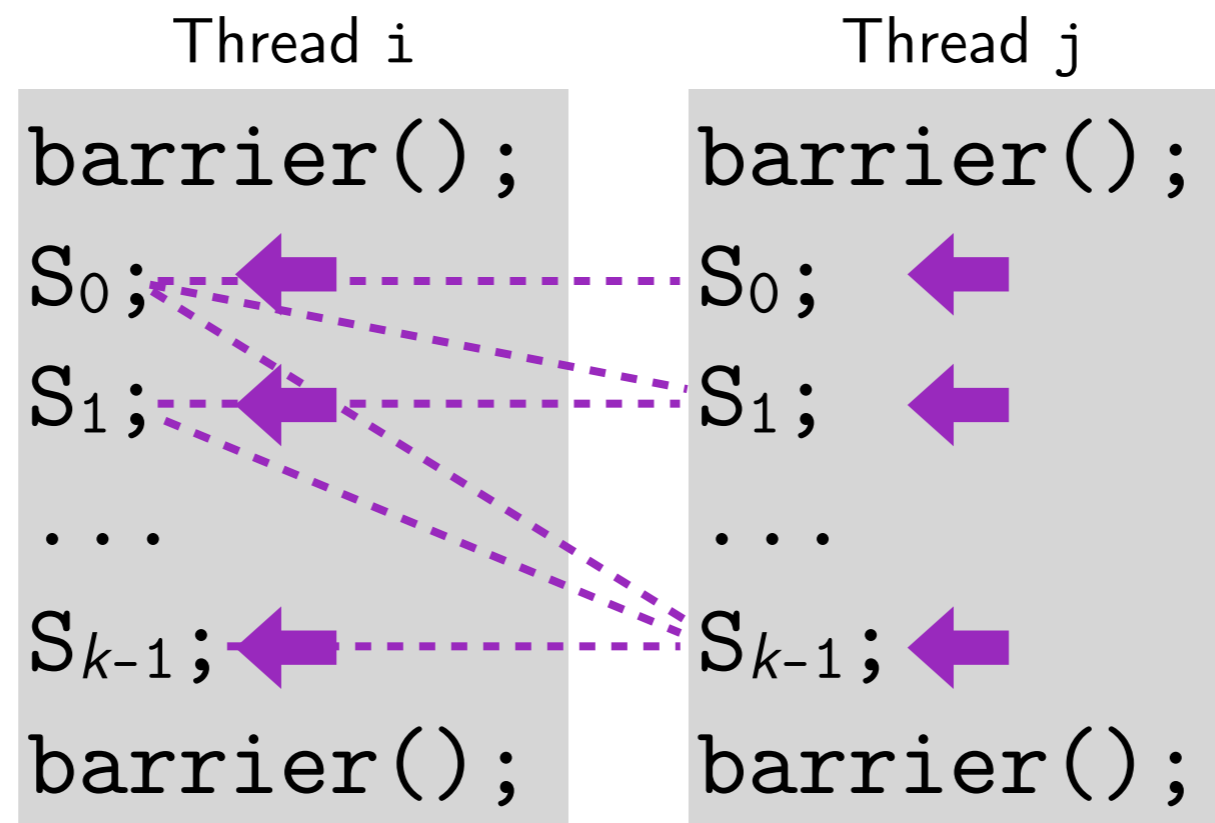
- ▶ There are about  $N^k$  possible interleavings ...  
but **any one of them** will do!



- ▶ Check each statement for races with the already-executed statements of all threads with lower tids

# Reduction to two threads

- ▶ We can do better still!
- ▶ Pick **arbitrary** threads  $i$  and  $j$  (ensuring  $i \neq j$ )



# Reduction to two threads

- ▶ We can do better still!
- ▶ Pick **arbitrary** threads  $i$  and  $j$  (ensuring  $i \neq j$ )
- ▶ Problem: it's like threads  $i$  and  $j$  are the **only threads**
- ▶ Account for the effects of other threads by **randomising the shared state** at each barrier

# Verification technique

► Plan:

Transform massively-parallel kernel **K**  
into a sequential program **P**  
such that if **P** is correct  
then **K** has no data races  
and no barrier divergence.

► Three key observations:

- any schedule will do
- two threads will do
- abstracting the shared state

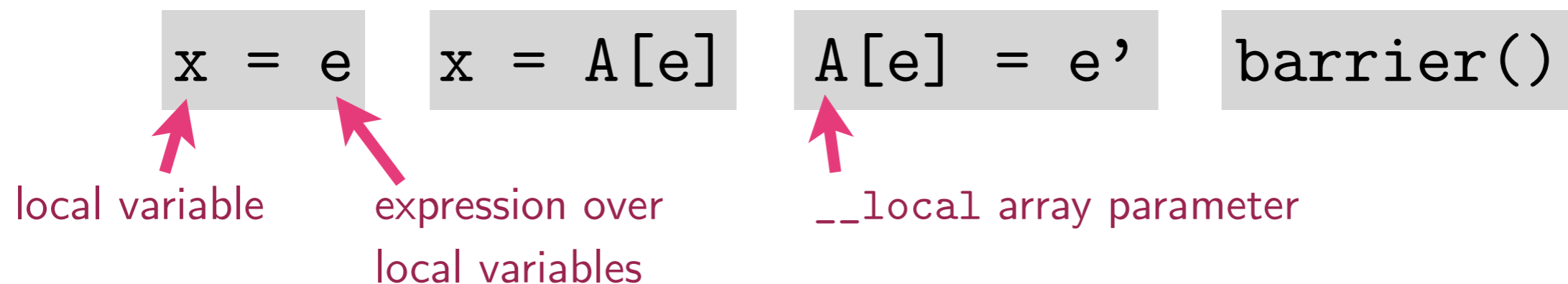
# Details of the two-thread reduction

# The two-thread reduction

- ▶ Assume kernel has this form:

```
__kernel void foo(<parameters>) {  
    <declare local variables>  
    S0; S1; . . . ; Sk-1;  
}
```

- ▶ where each statement  $S_k$  has one of these forms:



# Our example kernel

Kernel **K**:

```
__kernel void foo(  
    __local int* A,  
    __local int* B,  
    int idx)  
{  
    int x, y;  
    x = A[tid + idx];  
    y = A[tid];  
    A[tid] = x + y;  
}
```



# Picking two arbitrary threads

- ▶ Introduce two global variables:

```
var tid$1 : int;  
var tid$2 : int;
```

and assume that they are in-range and different:

```
requires 0 <= tid$1 && tid$1 < N;  
requires 0 <= tid$2 && tid$2 < N;  
requires tid$1 != tid$2;
```

# Logging reads and writes

- ▶ Replace each `__local` array parameter `A` with four global variables:

```
var READ_HAS_OCCURRED_A : bool;  
var WRITE_HAS_OCCURRED_A : bool;  
var READ_OFFSET_A : int;  
var WRITE_OFFSET_A : int;
```

- ▶ and four procedures:

```
procedure LOG_READ_A(offset : int);  
procedure LOG_WRITE_A(offset : int);  
procedure CHECK_READ_A(offset : int);  
procedure CHECK_WRITE_A(offset : int);
```

# The transformation so far...

Kernel **K**:

```
__kernel void foo(  
  __local int* A,  
  __local int* B,  
  int idx)  
{  
  ...  
}
```

Sequential program **P**:

```
var tid$1, tid$2 : int;  
var READ_HAS_OCCURRED_A : bool;  
var READ_HAS_OCCURRED_B : bool;  
var WRITE_HAS_OCCURRED_A : bool;  
var WRITE_HAS_OCCURRED_B : bool;  
var READ_OFFSET_A, READ_OFFSET_B : int;  
var WRITE_OFFSET_A, WRITE_OFFSET_B : int;  
procedure foo(idx : int)  
  requires 0 <= tid$1 && tid$1 < N;  
  requires 0 <= tid$2 && tid$2 < N;  
  requires tid$1 != tid$2;  
{  
  ...  
}
```

# Duplicating local variables

- ▶ Both threads need a copy of each local variable
- ▶ E.g. `int x;` becomes `var x$1, x$2 : int;`
- ▶ Same goes for non-array parameters
- ▶ Note that the values of the parameters are the same across all threads:

```
requires param$1 == param$2;
```

# Translating statements

S	translate(S)
<code>x = e;</code>	<code>x\$1 := e\$1;</code> <code>x\$2 := e\$2;</code>
<code>x = A[e];</code>	<code>call LOG_READ_A(e\$1);</code> <code>call CHECK_READ_A(e\$2);</code> <code>havoc x\$1, x\$2;</code>
<code>A[e] = e';</code>	<code>call LOG_WRITE_A(e\$1);</code> <code>call CHECK_WRITE_A(e\$2);</code>
<code>barrier();</code>	<code>call barrier();</code>
<code>S<sub>1</sub>; S<sub>2</sub>;</code>	<code>translate(S<sub>1</sub>); translate(S<sub>2</sub>);</code>

# The transformation so far...

Kernel **K**:

```
__kernel void foo(  
    __local int* A,  
    __local int* B,  
    int idx)  
{  
    int x, y;  
    x = A[tid + idx];  
    y = A[tid];  
    A[tid] = x + y;  
}
```

Sequential program **P**:

```
var tid$1, tid$2 : int;  
var READ_HAS_OCCURRED_A : bool;  
var READ_HAS_OCCURRED_B : bool;  
var WRITE_HAS_OCCURRED_A : bool;  
var WRITE_HAS_OCCURRED_B : bool;  
var READ_OFFSET_A, READ_OFFSET_B : int;  
var WRITE_OFFSET_A, WRITE_OFFSET_B : int;  
procedure foo(idx$1 : int, idx$2 : int)  
    requires 0 <= tid$1 && tid$1 < N;  
    requires 0 <= tid$2 && tid$2 < N;  
    requires tid$1 != tid$2;  
    requires idx$1 == idx$2;  
{  
    var x$1, x$2, y$1, y$2 : int;  
    call LOG_READ_A(tid$1 + idx$1);  
    call CHECK_READ_A(tid$2 + idx$2);  
    havoc x$1, x$2;  
  
    call LOG_READ_A(tid$1);  
    call CHECK_READ_A(tid$2);  
    havoc y$1, y$2;  
  
    call LOG_WRITE_A(tid$1);  
    call CHECK_WRITE_A(tid$2);  
}
```

# The logging functions

```
procedure LOG_READ_A(offset : int) {  
  if (*) {  
    READ_HAS_OCCURRED_A := true;  
    READ_OFFSET_A := offset;  
  }  
}
```

```
procedure LOG_WRITE_A(offset : int) {  
  if (*) {  
    WRITE_HAS_OCCURRED_A := true;  
    WRITE_OFFSET_A := offset;  
  }  
}
```

# The checking functions

```
procedure CHECK_READ_A(offset : int) {  
    assert (WRITE_HAS_OCCURRED_A ==> WRITE_OFFSET_A != offset);  
}
```

```
procedure CHECK_WRITE_A(offset : int) {  
    assert (WRITE_HAS_OCCURRED_A ==> WRITE_OFFSET_A != offset);  
    assert (READ_HAS_OCCURRED_A ==> READ_OFFSET_A != offset);  
}
```



# The transformation so far...

Kernel **K**:

```
__kernel void foo(  
    __local int* A,  
    __local int* B,  
    int idx)  
{  
    int x, y;  
    x = A[tid + idx];  
    y = A[tid];  
    A[tid] = x + y;  
}
```

Sequential program **P**:

```
var tid$1, tid$2 : int;  
var READ_HAS_OCCURRED_A : bool;  
var READ_HAS_OCCURRED_B : bool;  
var WRITE_HAS_OCCURRED_A : bool;  
var WRITE_HAS_OCCURRED_B : bool;  
var READ_OFFSET_A, READ_OFFSET_B : int;  
var WRITE_OFFSET_A, WRITE_OFFSET_B : int;  
procedure foo(idx$1 : int, idx$2 : int)  
    requires 0 <= tid$1 && tid$1 < N;  
    requires 0 <= tid$2 && tid$2 < N;  
    requires tid$1 != tid$2;  
    requires idx$1 == idx$2;  
    requires !READ_HAS_OCCURRED_A;  
    requires !WRITE_HAS_OCCURRED_A;  
{  
    var x$1, x$2, y$1, y$2 : int;  
    call LOG_READ_A(tid$1 + idx$1);  
    call CHECK_READ_A(tid$2 + idx$2);  
    havoc x$1, x$2;  
    call LOG_READ_A(tid$1);  
    call CHECK_READ_A(tid$2);  
    havoc y$1, y$2;  
    call LOG_WRITE_A(tid$1);  
    call CHECK_WRITE_A(tid$2);  
}
```

# Non-deterministic logging

```
var x$1, x$2, y$1, y$2 : int;  
call LOG_READ_A(tid$1 + idx$1);  
call CHECK_READ_A(tid$2 + idx$2);  
havoc x$1, x$2;  
call LOG_READ_A(tid$1);  
call CHECK_READ_A(tid$2);  
havoc y$1, y$2;  
call LOG_WRITE_A(tid$1);  
call CHECK_WRITE_A(tid$2);
```

# Non-deterministic logging

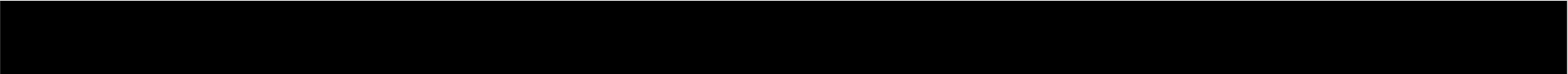
```
call LOG_READ_A(tid$1 + idx$1);  
call CHECK_READ_A(tid$2 + idx$2);  
call LOG_READ_A(tid$1);  
call CHECK_READ_A(tid$2);  
call LOG_WRITE_A(tid$1);  
call CHECK_WRITE_A(tid$2);
```

# Non-deterministic logging

```
//call LOG_READ_A(tid$1 + idx$1);
if (*) { READ_HAS_OCCURRED_A := true; READ_OFFSET_A := tid$1 + idx$1; }
//call CHECK_READ_A(tid$2 + idx$2);
assert (WRITE_HAS_OCCURRED_A ==> WRITE_OFFSET_A != tid$2 + idx$2);
//call LOG_READ_A(tid$1);
if (*) { READ_HAS_OCCURRED_A := true; READ_OFFSET_A := tid$1; }
//call CHECK_READ_A(tid$2);
assert (WRITE_HAS_OCCURRED_A ==> WRITE_OFFSET_A != tid$2)
//call LOG_WRITE_A(tid$1);
if (*) { WRITE_HAS_OCCURRED_A := true; WRITE_OFFSET_A := tid$1; }
//call CHECK_WRITE_A(tid$2);
assert (WRITE_HAS_OCCURRED_A ==> WRITE_OFFSET_A != tid$2);
assert (READ_HAS_OCCURRED_A ==> READ_OFFSET_A != tid$2);
```



# Non-deterministic logging

```
//call LOG_READ_A(tid$1 + idx$1);
if (*) { READ_HAS_OCCURRED_A := true; READ_OFFSET_A := tid$1 + idx$1; }
//call CHECK_READ_A(tid$2 + idx$2);
assert (WRITE_HAS_OCCURRED_A ==> WRITE_OFFSET_A != tid$2 + idx$2);
//call LOG_READ_A(tid$1);
if (*) {  }
//call CHECK_READ_A(tid$2);
assert (WRITE_HAS_OCCURRED_A ==> WRITE_OFFSET_A != tid$2)
//call LOG_WRITE_A(tid$1);
if (*) { WRITE_HAS_OCCURRED_A := true; WRITE_OFFSET_A := tid$1; }
//call CHECK_WRITE_A(tid$2);
assert (WRITE_HAS_OCCURRED_A ==> WRITE_OFFSET_A != tid$2);
assert (READ_HAS_OCCURRED_A ==> READ_OFFSET_A != tid$2);
```

# The `barrier()` function

```
procedure barrier() {  
    assume (!READ_HAS_OCCURRED_A);  
    assume (!WRITE_HAS_OCCURRED_A);  
    // Do this for every array  
}
```

# Summary so far

- ▶ For each array parameter  $A$ :
  - Add variables to log  $A$ 's reads and writes
  - Generate procedures to log and check reads and writes, using non-determinism to consider all possibilities
  - Remove  $A$ , and model reads from  $A$  using non-determinism
- ▶ For each statement in kernel  $\mathbf{K}$ :
  - generate corresponding statement(s) in sequential program  $\mathbf{P}$
  - interleave two arbitrary threads using round-robin schedule
- ▶ Next up: conditionals and loops



# Handling conditionals

- ▶ Use predicated execution to flatten **conditional code** into **straight line code**

```
if (x < 100) {  
    x = x+1;  
} else {  
    y = y+1;  
}
```



```
P := (x < 100);  
Q := !(x < 100);  
x := (P ? x+1 : x);  
y := (Q ? y+1 : y);
```

# Handling conditionals

- ▶ Use predicated execution to flatten **conditional code** into **straight line code**
- ▶ Each statement is tagged with a predicate that determines which threads are enabled
- ▶ This complicates the translation...

# Translating statements (revised)

S	translate(S,P)
<code>x = e;</code>	<code>x\$1 := P\$1 ? e\$1 : x\$1;</code> <code>x\$2 := P\$2 ? e\$2 : x\$2;</code>
<code>x = A[e];</code>	<code>call LOG_READ_A(P\$1, e\$1);</code> <code>call CHECK_READ_A(P\$2, e\$2);</code> <code>x\$1 := P\$1 ? * : x\$1;</code> <code>x\$2 := P\$2 ? * : x\$2;</code>
<code>A[e] = e';</code>	<code>call LOG_WRITE_A(P\$1, e\$1);</code> <code>call CHECK_WRITE_A(P\$2, e\$2);</code>
<code>barrier();</code>	<code>call barrier(P\$1, P\$2);</code>
<code>S<sub>1</sub>; S<sub>2</sub>;</code>	<code>translate(S<sub>1</sub>,P); translate(S<sub>2</sub>,P);</code>

S	translate(S,P)
<code>if(e) {</code> <code>S<sub>1</sub>;</code> <code>}</code> <code>else {</code> <code>S<sub>2</sub>;</code> <code>}</code>	<code>Q\$1 := P\$1 &amp;&amp; e\$1;</code> <code>Q\$2 := P\$2 &amp;&amp; e\$2;</code> <code>R\$1 := P\$1 &amp;&amp; !e\$1;</code> <code>R\$2 := P\$2 &amp;&amp; !e\$2;</code> <code>translate(S<sub>1</sub>,Q);</code> <code>translate(S<sub>2</sub>,R);</code>
<code>while(e) {</code> <code>S;</code> <code>}</code>	<code>Q\$1 := P\$1 &amp;&amp; e\$1;</code> <code>Q\$2 := P\$2 &amp;&amp; e\$2;</code> <code>while (Q\$1    Q\$2) {</code> <code>translate(S,Q);</code> <code>Q\$1 := P\$1 &amp;&amp; e\$1;</code> <code>Q\$2 := P\$2 &amp;&amp; e\$2;</code> <code>}</code>

# The logging functions (revised)

```
procedure LOG_READ_A(enabled : bool, offset : int) {  
  if (enabled && *) {  
    READ_HAS_OCCURRED_A := true;  
    READ_OFFSET_A := offset;  
  }  
}
```

```
procedure LOG_WRITE_A(enabled : bool, offset : int) {  
  if (enabled && *) {  
    WRITE_HAS_OCCURRED_A := true;  
    WRITE_OFFSET_A := offset;  
  }  
}
```

# The checking functions (revised)

```
procedure CHECK_READ_A(enabled : bool, offset : int) {  
    assert (enabled && WRITE_HAS_OCCURRED_A  
        ==> WRITE_OFFSET_A != offset);  
}
```

```
procedure CHECK_WRITE_A(enabled : bool, offset : int) {  
    assert (enabled && WRITE_HAS_OCCURRED_A  
        ==> WRITE_OFFSET_A != offset);  
    assert (enabled && WRITE_HAS_OCCURRED_A  
        ==> WRITE_OFFSET_A != offset);  
}
```

# The barrier() function (revised)

```
procedure barrier(enabled$1 : bool, enabled$2 : bool) {  
  assert (enabled$1 == enabled$2);  
  if (!enabled$1) return;  
  
  assume (!READ_HAS_OCCURRED_A);  
  assume (!WRITE_HAS_OCCURRED_A);  
  // Do this for every array  
}
```

# Find out more

- ▶ Download GPUVerify:
  - [multicore.doc.ic.ac.uk/tools/GPUVerify](http://multicore.doc.ic.ac.uk/tools/GPUVerify)
- ▶ Or try it online:
  - [rise4fun.com/GPUVerify-OpenCL](http://rise4fun.com/GPUVerify-OpenCL)
- ▶ The Multicore Group at Imperial
  - [multicore.doc.ic.ac.uk](http://multicore.doc.ic.ac.uk)

# Further reading

- A. Betts, N. Chong, A. Donaldson, S. Qadeer, P. Thomson. *GPUVerify, a verifier for GPU kernels*, **OOPSLA 2012**
- P. Collingbourne, A. Donaldson, J. Ketema, S. Qadeer. *Interleaving and lock-step semantics for analysis and verification of GPU kernels*, **ESOP 2013**
- G. Li, G. Gopalakrishnan. *Scalable SMT-based verification of GPU kernel functions*, **FSE 2010**
- G. Li, P. Li, G. Sawaya, G. Gopalakrishnan, I. Ghosh, S. Rajan. *GKLEE: Concolic verification and test generation for GPUs*, **PPoPP 2012**
- A. Leung, M. Gupta, Y. Agarwal, R. Gupta, R. Jhala, S. Lerner. *Verifying GPU kernels by test amplification*, **PLDI 2012**.